



## Lagrange model for the chiral optical properties of stereometamaterials

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(Received 16 April 2010; revised manuscript received 14 May 2010; published 4 June 2010)

We employ a general Lagrange model to describe the chiral optical properties of stereometamaterials. We derive the elliptical eigenstates of a twisted stacked split-ring resonator taking phase retardation into account. Through this approach, we obtain a powerful Jones matrix formalism which can be used to calculate the polarization rotation, ellipticity, and circular dichroism of transmitted waves through stereometamaterials at any incident polarization. Our experimental measurements agree well with our model.

DOI: [10.1103/PhysRevB.81.241403](https://doi.org/10.1103/PhysRevB.81.241403)

PACS number(s): 78.67.Bf, 73.20.Mf, 78.20.Ek, 41.20.Jb

Stereo in Greek means spatial or three dimensional (3D). Stereometamaterials are three-dimensional nanostructures with characteristic dimensions much smaller than the wavelength of light.<sup>1</sup> Examples of stereometamaterials include stacked wires,<sup>2</sup> crosses,<sup>3</sup> gammadians,<sup>4</sup> and spirals.<sup>5</sup> One specific type of stereometamaterials are stacked and twisted split-ring resonators (SRRs).<sup>6–9</sup> In particular, upon twisting of the two individual split rings at angles other than 0° and 180°, such a stereometamaterial can form left- or right-handed enantiomers, which might exhibit chiral optical properties. In analogy to stereochemistry,<sup>10</sup> the transmission and reflection properties of stereometamaterials can be measured with linearly and circularly polarized light at different wavelengths, and quantities such as circular dichroism (CD), polarization rotation, and ellipticity can be determined experimentally.

A convenient description of the polarization properties of optical elements at normal incidence is the Jones calculus, which connects the input and output polarization vector of light by a  $2 \times 2$  matrix. The polarization eigenstates are the eigenvectors of that Jones matrix. In order to design future polarization elements composed of nano-optical components, one requires a simple coupling model which allows for intuitive understanding, as well as for the calculation and application of the polarization properties in nanophotonic stereometamaterials.

In this Rapid Communication, we provide such a model. Namely, we introduce a Lagrange model that takes the individual oscillators of our stereometamaterial plus important coupling processes into account. In particular, we treat electric and magnetic coupling separately. Importantly, we include phase retardation, which is essential for stacked structures. It arises from the light propagation along the stacked individual elements as well as from the resonant behavior of the SRR elements. We are able to determine the chiral optical eigenmodes. This allows us to describe even very complex structures such as multilayer twisted structures with large spacer distances as described in Ref. 11. For a planar structure without the phase retardation effect, the two eigenwaves will degrade to linear polarization and optical activity at normal incidence will disappear. Our model will allow tuning of

the polarization properties in complex coupled 3D systems, such as nanospirals, to a set of desired parameters and enable, for example, broadband operation of such spirals as near-achromatic wave retarders.<sup>12</sup>

In principle, *ab initio* methods such as finite-difference time domain (FDTD) method, S matrix,<sup>13</sup> and others, are able to predict the polarization properties of stereometamaterials. However, these methods solve Maxwell's equations numerically and do not provide deeper insight into the intricate coupling mechanisms.

Figure 1 displays the geometry of our stereometamaterial together with the design parameters. Each unit cell is composed of two separate SRRs, which are twisted at by an angle  $\theta$  with respect to one another. The twist angle varies from 0° to 180°. The SRRs are embedded in a homogeneous dielectric with  $n=1.55$  (our spacer material PC403) and reside on a glass substrate ( $n=1.51$ ). The incident electromagnetic (EM) wave is normal to the SRRs and propagates in the  $z$  direction as shown in Fig. 1. To study the electromagnetic (EM) response of the stereo-SRR metamaterial, we rely on a full wave simulation using a time-domain simulation software (CST MICROWAVE STUDIO). In the simulation, the metal permittivity is given by  $\epsilon(\omega) = 1 - \omega_p^2 / (\omega^2 + i\omega\tau)$ , where  $\omega_p$

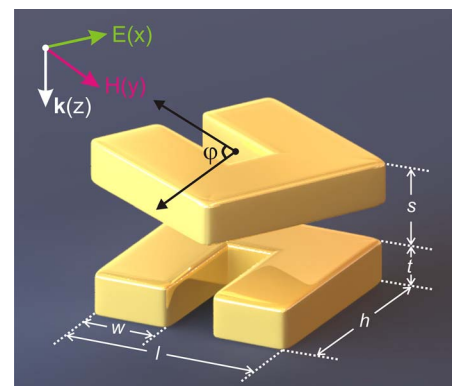


FIG. 1. (Color online) Schematic of the stereo-SRR dimer metamaterial with definitions of the geometrical parameters:  $l = 230$  nm,  $h = 230$  nm,  $w = 90$  nm,  $t = 50$  nm, and  $s = 100$  nm. The periods in both  $x$  and  $y$  directions are 700 nm.

is the bulk plasma frequency and  $\omega_p$  is the relaxation rate. For gold, the characteristic frequencies fitted to experimental data are  $\omega_p = 1.37 \times 10^4$  THz and  $\omega_r = 40.84$  THz.<sup>14</sup>

A single SRR consists of a magnetic loop (the metal ring) with inductance  $L$  and a capacitor with capacitance  $C$  (corresponding to the slit). Thus it can be modeled by an ideal  $L$ - $C$  circuit with resonance frequency  $\omega_0 = 1/\sqrt{LC}$ , for which the Lagrangian can be written as  $\mathcal{L}_0 = L(\dot{Q}^2 - \omega_0^2 Q^2)/2$ . Here the total oscillatory charge  $Q$  accumulated in the gap is defined as a generalized coordinate,  $L\dot{Q}^2/2$  is the kinetic energy of the oscillations, and  $L\omega_0^2 Q^2/2$  refers to the electrostatic energy stored in the gap. In the hybridization model, each SRR can be regarded as an artificial atom while the stereo-SRR system represents an artificial molecule. When excited by an incident EM wave, the Lagrangian of the stereo-SRR metamaterial can be rewritten as

$$\begin{aligned} \mathcal{L} = & L(\dot{Q}_1^2 - \omega_0^2 Q_1^2)/2 + L(\dot{Q}_2^2 - \omega_0^2 Q_2^2)/2 + M_m \dot{Q}_1 \dot{Q}_2 \\ & - M_e \omega_0^2 Q_1 Q_2 \cdot (\cos \theta - \alpha \cdot \cos^2 \theta + \beta \cdot \cos^3 \theta) \\ & - \mathbf{P}_1 \cdot \mathbf{E} - \mathbf{P}_2 \cdot \mathbf{E} \cdot e^{i\varphi}. \end{aligned} \quad (1)$$

The first two terms of Eq. (1) give the energy stored in the two SRRs while the last two terms are the magnetic and electric interaction energy between them. The contributions of the electric quadrupolar and octupolar interactions are considered as correction terms of the electric dipolar action with coefficients  $\alpha$  and  $\beta$ , respectively.  $\mathbf{P}_1 = l_{eff} \cdot \hat{\mathbf{x}} \cdot Q_1$  and  $\mathbf{P}_2 = l_{eff} \cdot (\cos \theta \cdot \hat{\mathbf{x}} - \sin \theta \cdot \hat{\mathbf{y}}) \cdot Q_2$  are the induced electric dipole moments in the gap of two SRRs ( $l_{eff}$  is the effective length of the single SRR),  $\varphi$  is the phase retardation which arises due to the distance between two stacked SRRs in the propagation direction and due to the resonant behavior of the SRR elements. According to Ref. 6, the two eigenfrequencies of the stereo-SRR metamaterial are obtained as:  $\omega_- = \omega_0 \cdot \sqrt{(1 + \kappa_e)/(1 + \kappa_m)}$  and  $\omega_+ = \omega_0 \cdot \sqrt{(1 - \kappa_e)/(1 - \kappa_m)}$ , where  $\kappa_m = M_m/L$  and  $\kappa_e = M_e \cdot (\cos \theta - \alpha \cdot \cos^2 \theta + \beta \cdot \cos^3 \theta)/L$  are the magnetic and electric coupling coefficients, respectively. The magnetic coupling possesses rotational symmetry and is not twist angle dependent (see supplement). The electric interaction of the stereo-SRR metamaterial is closely related to the spatial arrangement of the metamaterial elements. Fitting the twist dispersion curves yields the corresponding coefficients as  $\kappa_m = M_m/L = 0.09$ ,  $\kappa'_e = M_e/L = 0.14$ ,  $\alpha = 0.8$ , and  $\beta = -0.4$ .

By introducing the Ohmic dissipation  $\mathfrak{R} = \sigma(\dot{Q}_1^2 + \dot{Q}_2^2)/2$  and substituting it into the Euler-Lagrange equations,

$$(d/dt)(\partial \mathcal{L} / \partial \dot{Q}_i) - \partial \mathcal{L} / \partial Q_i = -\partial \mathfrak{R} / \partial \dot{Q}_i \quad (i = 1, 2), \quad (2)$$

we obtain the solutions for  $Q_i$  ( $i = 1, 2$ ).<sup>15</sup> Based on the material equations  $\mathbf{P} = \mathbf{P}_1 + \mathbf{P}_2 = \chi \mathbf{E} = (1 - \varepsilon) \mathbf{E}$  and combining them with the definition of  $\mathbf{P}$  in Eq. (1), the elements of the effective permittivity tensor for the stereo-SRR metamaterial can be obtained as in Ref. 15. According to the wave equation  $\mathbf{k} \times (\mathbf{k} \times \mathbf{E}) + \omega^2 \varepsilon \mu \cdot \mathbf{E} = 0$ , the refractive indices of the two eigenmodes of such a stereo-SRR metamaterial are given as

$$n_{\pm} = \sqrt{(\varepsilon_{xx} + \varepsilon_{yy} \pm \sqrt{(\varepsilon_{xx} - \varepsilon_{yy})^2 + 4\varepsilon_{xy}\varepsilon_{yx}})/2}. \quad (3)$$

The corresponding polarization states of these two eigenmodes are represented by the following Jones vectors:

$$\begin{aligned} \mathbf{J}_- &= \frac{1}{\mathcal{N}_-} \begin{pmatrix} -2\varepsilon_{yx} \\ (\varepsilon_{xx} - \varepsilon_{yy}) + \sqrt{(\varepsilon_{xx} - \varepsilon_{yy})^2 + 4\varepsilon_{xy}\varepsilon_{yx}} \end{pmatrix}, \\ \mathbf{J}_+ &= \frac{1}{\mathcal{N}_+} \begin{pmatrix} -2\varepsilon_{xy} \\ (\varepsilon_{xx} - \varepsilon_{yy}) - \sqrt{(\varepsilon_{xx} - \varepsilon_{yy})^2 + 4\varepsilon_{xy}\varepsilon_{yx}} \end{pmatrix}, \end{aligned} \quad (4)$$

where  $\mathcal{N}_{\pm}$  are the corresponding normalized coefficients. Similar to Condon's theory,<sup>16</sup> these two Jones vectors present two orthogonal elliptically polarized states  $\mathbf{J}_- \cdot \mathbf{J}_+ = 0$ . For these two eigenmodes, the corresponding transmission coefficients through the stereometamaterial can be obtained as<sup>17</sup>

$$t_{\pm} = \frac{4n_{\pm} \exp(-in_{\pm}kd)}{(n_{\pm} + 1)^2 - (n_{\pm} - 1)^2 \exp(-2in_{\pm}kd)}. \quad (5)$$

Any state in the  $x$ - $y$  coordinate system can be transformed into the principal  $\mathbf{J}_+$ - $\mathbf{J}_-$  coordinate system. Therefore, the transmission coefficient for any incident wave  $\begin{pmatrix} E_x^i \\ E_y^i \end{pmatrix}$  can be calculated as

$$\begin{aligned} \begin{pmatrix} E_x^t \\ E_y^t \end{pmatrix} &= \mathbf{T} \cdot \begin{pmatrix} E_x^i \\ E_y^i \end{pmatrix} \\ &= \begin{pmatrix} \hat{x} \cdot \mathbf{J}_+ & \hat{x} \cdot \mathbf{J}_- \\ \hat{y} \cdot \mathbf{J}_+ & \hat{y} \cdot \mathbf{J}_- \end{pmatrix} \cdot \begin{pmatrix} t_+ & 0 \\ 0 & t_- \end{pmatrix} \cdot \begin{pmatrix} \hat{x} \cdot \mathbf{J}_+ & \hat{y} \cdot \mathbf{J}_+ \\ \hat{x} \cdot \mathbf{J}_- & \hat{y} \cdot \mathbf{J}_- \end{pmatrix} \cdot \begin{pmatrix} E_x^i \\ E_y^i \end{pmatrix}. \end{aligned} \quad (6)$$

Here,  $\mathbf{T}$  is the Jones matrix which is used to determine the polarization state of the transmission wave through the stereometamaterial. Equation (6) is a very powerful result. In principle, based on this equation, we can calculate not only the transmission of the stereometamaterials but also the polarization states of transmitted waves with different incident polarization for any frequency. Our stereometamaterial can therefore be replaced by a black box which describes an artificial polarization element with a certain Jones matrix  $\mathbf{J}_+$  and  $\mathbf{J}_-$ .<sup>15</sup>

For the linearly polarized incident case  $\begin{pmatrix} 1 \\ 0 \end{pmatrix}$ , the transmitted wave is  $\begin{pmatrix} t_- \hat{x} \cdot \mathbf{J}_+ \hat{x} \cdot \mathbf{J}_+ + t_+ \hat{x} \cdot \mathbf{J}_- \hat{x} \cdot \mathbf{J}_- \\ t_+ \hat{y} \cdot \mathbf{J}_+ \hat{x} \cdot \mathbf{J}_+ + t_- \hat{y} \cdot \mathbf{J}_- \hat{x} \cdot \mathbf{J}_- \end{pmatrix}$ . The polarization state of the transmitted wave will change accordingly. For any other polarized wave, such as left-handed and right-handed circularly polarized (LCP and RCP) waves, the polarization state of the transmission wave can also be calculated directly based on the above Jones matrix model.

For stereo-SRR structures with different twist angles  $\theta$ , the optical response is quite different. For the cases  $\theta = 0^\circ$  and  $180^\circ$ ,  $\varepsilon_{xy} = \varepsilon_{yx} = 0$ ,  $\varepsilon_{yy} = 1$ ,  $\varepsilon_{xx} \neq 1$ , only the  $x$ -polarization resonance can be excited. Correspondingly,  $n_+ = \sqrt{\varepsilon_{xx}}$ ,  $n_- = 1$ ,  $\mathbf{J}_+ = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$ , and  $\mathbf{J}_- = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$ . For the case  $\theta = 90^\circ$ , the refractive indices of the two eigenmodes and the corresponding eigen-wave vectors are calculated as

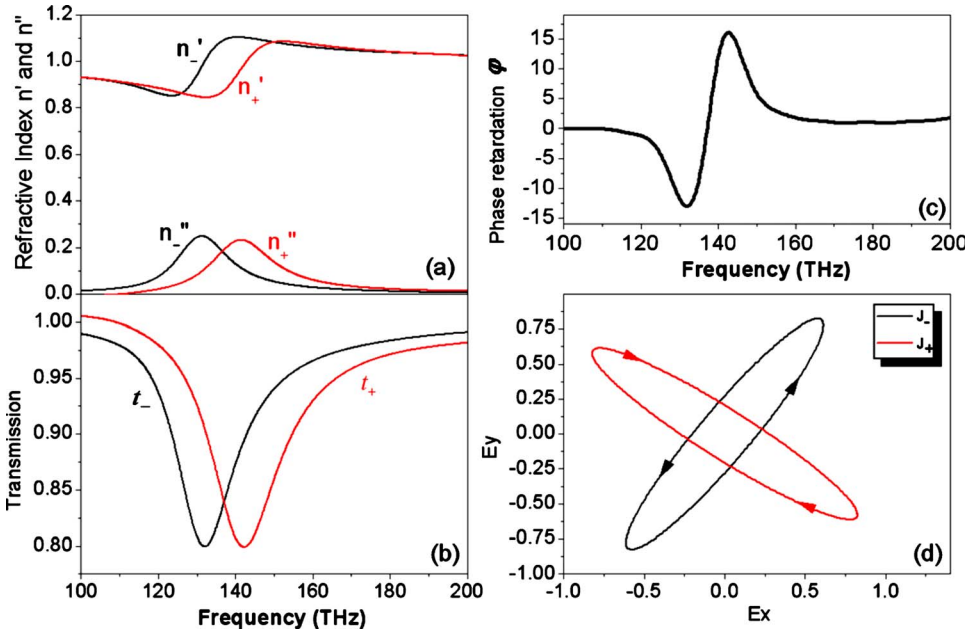


FIG. 2. (Color online) (a) Refractive index of two eigenmodes in a  $90^\circ$  twisted SRR stereometamaterial (Lagrange model); (b) transmission of two eigenmodes (Lagrange model); (c) phase retardation (FDTD simulation); and (d) two elliptical polarization states of two eigenmodes at a frequency of 140 THz (Lagrange model).

$$n_{\pm} = \sqrt{1 + \frac{(1 + e^{i\varphi})\ell(\omega^2 - i\gamma\omega - \omega_0^2) \pm \ell\sqrt{(1 - e^{i\varphi})^2(\omega^2 - i\gamma\omega - \omega_0^2)^2 + 4\kappa_m^2\omega^4 e^{i\varphi}}}{2(1 - \kappa_m^2) \cdot (\omega^2 - i\gamma_-\omega - \omega_-^2) \cdot (\omega^2 - i\gamma_+\omega - \omega_+^2)}}, \quad (7)$$

$$\mathbf{J}_- = \frac{1}{N_-} \left( (1 - e^{i\varphi})(\omega^2 - i\gamma\omega - \omega_0^2) + \frac{-2\kappa_m\omega^2}{\sqrt{(1 - e^{i\varphi})^2(\omega^2 - i\gamma\omega - \omega_0^2)^2 + 4\kappa_m^2\omega^4 e^{i\varphi}}} \right), \quad (8)$$

$$\mathbf{J}_+ = \frac{1}{N_+} \left( (1 - e^{i\varphi})(\omega^2 - i\gamma\omega - \omega_0^2) - \frac{2\kappa_m\omega^2 e^{i\varphi}}{\sqrt{(1 - e^{i\varphi})^2(\omega^2 - i\gamma\omega - \omega_0^2)^2 + 4\kappa_m^2\omega^4 e^{i\varphi}}} \right).$$

Here,  $\ell = l_{eff}T = l_{eff}^2/L$ ,  $\gamma = \sigma/L$ ,  $\gamma_- = \gamma/(1 + \kappa_m)$ , and  $\gamma_+ = \gamma/(1 - \kappa_m)$ . In order to visualize the above analytical results, we plot the  $n_{\pm}$  in Fig. 2(a). Equation (8) implies that we have varying eigenvectors  $\mathbf{J}_{\pm}$  with varying polarization state at different incident frequencies. For example, at 140 THz, the two eigenmodes are ellipses as plotted in Fig. 2(d).

For a planar structure, there is no phase retardation effect between two SRRs. The phase retardation  $\varphi$  equals zero, and hence the two eigenmodes  $\mathbf{J}_{\pm}$  are linearly polarized. For the stereo-SRR structure, the calculated value for  $\varphi$  is displayed in Fig. 2(c). Obviously,  $\varphi$  is not equal to zero around the resonance frequencies and hence the eigenstates are not linearly polarized. Therefore, the phase retardation  $\varphi$  is the decisive parameter that distinguishes stereometamaterials from planar metamaterials with respect to their chiral optical properties. Furthermore, we can change the phase retardation  $\varphi$  by changing the coupling distance. As a result, the eigenmodes of stereometamaterials and their propagation properties can also be tuned this way.

For any other incident polarized wave  $\mathbf{E} = \begin{pmatrix} E_x \\ E_y \end{pmatrix}$ , which can be regarded as the combination of two eigenwaves  $\begin{pmatrix} E_x \\ E_y \end{pmatrix} = a_- \mathbf{J}_- + a_+ \mathbf{J}_+$ , two eigenmodes are excited simultaneously. Therefore, the wave will change its polarization state at both

resonance frequencies  $\omega_+$  and  $\omega_-$ . In particular, we can expand the LCP and RCP in our coordinate system with the two axes  $\mathbf{J}_-$  and  $\mathbf{J}_+$ :  $\mathbf{E}_{LCP} = 1/\sqrt{2} \begin{pmatrix} 1 \\ -i \end{pmatrix} = a_-^{LCP} \mathbf{J}_- + a_+^{LCP} \mathbf{J}_+$ ,  $\mathbf{E}_{RCP} = 1/\sqrt{2} \begin{pmatrix} 1 \\ i \end{pmatrix} = a_-^{RCP} \mathbf{J}_- + a_+^{RCP} \mathbf{J}_+$ . According to Eq. (8), we know that  $\mathbf{J}_{\pm}$  shows strong frequency dependence, especially at  $\omega_{\pm}$ . Therefore, the coefficients  $a_-^{LCP}$ ,  $a_+^{LCP}$ ,  $a_-^{RCP}$ , and  $a_+^{RCP}$  will depend on the incident frequency. For example, at  $\omega = 140$  THz, the calculated results are  $a_-^{LCP} = -0.497 + i0.365$ ,  $a_+^{LCP} = 0.365 + i0.497$ ,  $a_-^{RCP} = -0.654 - i0.479$ , and  $a_+^{RCP} = 0.497 - i0.654$ . The transmission of LCP and RCP light can be calculated according to Eq. (6) and is plotted in Figs. 3(c) and 3(f). Additionally, the circular dichroism  $t_{CD} = t_{RCP} - t_{LCP}$  is displayed in Fig. 3(i). It is quite interesting that  $t_{CD}$  shows a dip around the lower resonance frequency  $\omega_-$  and a peak around the higher resonance frequency  $\omega_+$ . The reason is as follows: LCP light is composed of a larger part of  $\mathbf{J}_-$  (which is left-handedly polarized and experiences more absorption at  $\omega_-$  than  $\omega_+$ ) than  $\mathbf{J}_+$  (which is right-handed polarized and possesses higher absorption at  $\omega_+$  than at  $\omega_-$ ). Therefore, RCP light possesses a larger resonance absorption at  $\omega_-$  than  $\omega_+$ : hence  $t_{RCP}(\omega_-) < t_{RCP}(\omega_+)$ . Reversely, LCP experiences a larger resonance absorption at  $\omega_+$  than  $\omega_-$ , hence  $t_{RCP}(\omega_-) > t_{RCP}(\omega_+)$ . Therefore, we can conclude that

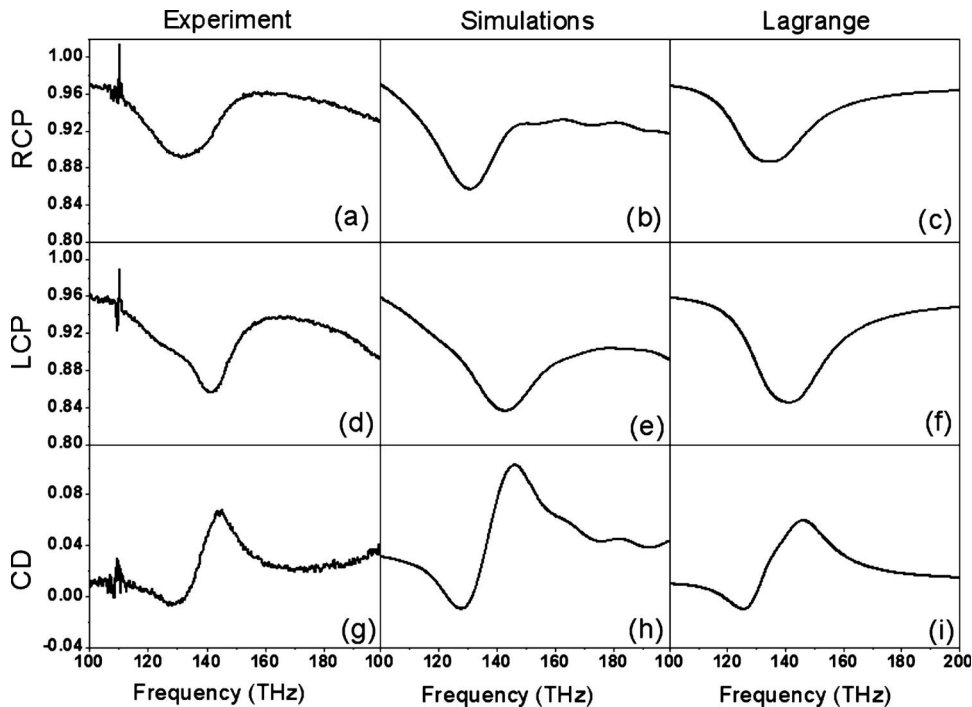


FIG. 3. [(a)–(f)] Transmission of LCP and RCP light through stereometamaterials; [(g)–(i)] CD (LCP-RCP) of stereometamaterials. [(a), (d), and (g)] Experimental results; [(b), (e), and (h)] simulated (FDTD) results; and [(c), (f), and (i)] analytical Lagrange model results).

the circular dichroism satisfies  $t_{CD}(\omega_-) < t_{CD}(\omega_+)$ , which explains the results in Fig. 3 very well. In order to verify the above Jones matrix formalism, we fabricated the stereo-SRR structure in Fig. 1 with the method reported in Ref. 6. The measured transmission of RCP and LCP light, as well as the circular dichroism are given in Figs. 3(a), 3(d), and 3(g). We also plotted the FDTD simulations results for the same structures, which are plotted in Figs. 3(b), 3(e), and 3(h). The comparison shows that all three results agree quite well with each other. This proves that our Lagrange model is quite successful in describing the optical polarization properties of stereometamaterials.

Besides circularly polarized light, the Jones matrix formalism can also be used to calculate the polarization rotation and ellipticity of transmitted waves for any other kind of incident polarized wave. Furthermore, the Lagrange theory is not only used to calculate the optical activity in the structure given in Fig. 1 but can also be applied to many other metamaterials and plasmonic systems, such as spiral springs,<sup>5</sup> gammadions,<sup>4</sup> crosses,<sup>3</sup> and more complex structures.<sup>2,18</sup>

In summary, we presented a Lagrange model to investigate the chiral optical properties of stereometamaterials. The phase retardation effect due to the three-dimensional stacked configuration is taken into consideration. Two elliptical eigenwaves are obtained which are the basis vectors of the Jones matrix of the stereometamaterial. The polarization change for any polarized incident wave can be calculated with such a Jones matrix formalism. A stereometamaterial of twisted SRRs was fabricated and the measured circular dichroism agrees well with our theoretical calculations. This work will stimulate many related investigations on other complex 3D nanostructures.

This work was supported by the National Natural Science Foundation of China (Grant Nos. 10704036, 10874081, 60907009, 10904012, 10974090, and 60990320), and by the National Key Projects for Basic Researches of China (Grant Nos. 2006CB921804, 2009CB930501, and 2010CB630703), as well as by DFG (FOR 557) and BMBF (3D Metamat).

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<sup>15</sup>See supplementary material at <http://link.aps.org/supplemental/10.1103/PhysRevB.81.241403> for Jones matrix formalism based on Lagrange model provided by H. Liu, J. X. Cao, S. N. Zhu, N. Liu, R. Ameling, and H. Giessen.

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